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Supra soft π g-closed sets in soft supra topological spaces

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Abstract

We introduce the concept of supra soft π g-closed sets in soft supra topological spaces and we discuss their relationships. Also we discuss their relationships with other supra- soft closed set in detail, supported by examples and counter examples. Further we investigated supra-soft π g separateness and connectedness in soft supra topological space.

Keywords: Supra soft π g- closed sets, Supra soft- π g-connected, Supra soft- π g-separateness

1. Introduction

In 1999, Molodtsov ^[12] proposed the concept of a soft set which can be seen as a new mathematical approach to vagueness. In fact, a soft set is a parameterized family of subsets of a given universe set. The way of parameterization in problem solving makes soft set theory convenient and simple for application. Maji *et al.* ^[10] carried out Molodtsov's idea by introducing several operations in soft set theory. Shabir and Naz ^[12] presented soft topological spaces and they investigated some properties of them. Later, many mathematicians ^[3, 6, 7, 8, 11, 14] studied some of basic concepts and properties of soft topological spaces.

El-Sheikh and Abd El-Latif ^[5] introduced the concept of supra soft topological spaces, which is wider and more general than the class of soft topological spaces. They introduced a unification of some types of different kinds of subsets of supra soft topological spaces using the notion of γ -operation and studied the decompositions of some forms of supra soft continuity. After then, Kandil *et al.* ^[7] studied the concepts of supra generalized closed soft sets and supra generalized closed soft sets with respect to a soft ideal in a supra topological space. To develop soft set theory, the operations of the soft sets are redefined and a uni-int decision making method was constructed by using these new operations ^[3]. Recently, K. Kannan ^[9] introduced the concept of g-closed soft sets in a soft topological spaces. El-sheikh and Abd El-latif ^[3] have extended the notions of g-closed soft sets to supra soft topological spaces. In this paper we introduce and study the concepts of supra soft π g- closed sets in supra soft topological spaces. Also we present supra soft- π g separateness and connectedness in soft supra topological space.

2. Preliminaries

Let X be an initial universe set and E be the set of all possible parameters with respect to X. parameters are often attributes, characteristics or properties of the objects in X. let P(X) denote the power set of X, then a soft set over X is defined as follows.

Definition [2.1] ^[1]

A pair (F, A) is called a soft set over U where $A \subseteq E$ and $F: A \rightarrow P(U)$ is a set valued mapping. In other words, a soft set over X is a parameterized family of subsets of the universe U. For $\forall e \in A$, F(e) may be considered as the set of e -approximate elements of the soft set (F,A). It is worth noting that F(e) may be arbitrary. Some of them may be empty, and some may have nonempty intersection.

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Definition [2.2] ^[13]

A soft set (F,A) over U is said to be a null soft set denoted by \emptyset if for all $e \in A$, $F(e) = \emptyset$. A soft set (F, A) over U is said to be an absolute soft set denoted by A if for all $e \in A$, $F(e) = U$.

Definition [2.3] ^[2]

Let Y be a nonempty subset of X, then \tilde{Y} denotes the soft set (Y, E) over X for which $Y(e) = Y$, for all $e \in E$. In particular, (X, E) will be denoted by \tilde{X} .

Definition [2.4] ^[2]

For two soft sets (F, A) and (G, B) over U, we say that (F,A) is a soft subset of (G, B) if $A \subseteq B$ and for all $e \in A$, $F(e)$ and $G(e)$ are identical approximations. We write (F,A) \subseteq (G,B). (F,A) is said to be a soft super set of(G,B), if (G,B) is a soft subset of (F, A). We denote it by (G,B) \subseteq (F, A). Then(F,A) and (G,B) are said to be soft equal if (F,A) is a soft subset of (G,B) and(G,B) is a soft subset of (F,A).

Definition [2.5] ^[13]

For two soft sets (F,A) and (G,B) over a common universe U.

The union of two soft sets (F,A) and (G,B) is the soft set (H,C), where $C = A \cup B$ and for all $e \in C$,

$$H(e) = \begin{cases} F(e) & , \text{if } e \in A - B \\ G(e) & , \text{if } e \in B - A \\ F(e) \cup G(e) & , \text{if } e \in A \cap B \end{cases}$$

We write (F,A) \cup (G,B)=(H,C).

Definition [2.6] ^[2]

The intersection (H, C) of two soft sets (F, A) and (G,B) over a common universe U denoted (F,A) \cap (G,B) is defined as $C = A \cap B$ and $H(e) = F(e) \cap G(e)$, for all $e \in C$.

Definition [2.7] ^[4]

For a soft set (F, A) over the universe U, the relative complement of (F, A) is denoted by $(F,A)^c$ and is defined by $(F,A)^c = (F^c, A)$, where $F^c: A \rightarrow P(U)$ is a mapping defined by $F^c(e) = U - F(e)$, for all $e \in A$.

Definition [2.8] ^[2]

Let $\tilde{\tau}$ be the collection of soft sets over a universe U with a fixed set of parameters E, then $\tilde{\tau}$ is said to be a soft topology on U.

- 1) $\emptyset, U \in \tilde{\tau}$
- 2) The union of any number of soft sets in $\tilde{\tau}$ belongs to $\tilde{\tau}$.
- 3) The intersection of any two soft sets in $\tilde{\tau}$ belongs to $\tilde{\tau}$.

The triplet (U, $\tilde{\tau}$, E) is called a soft topological space. Every member of $\tilde{\tau}$ is

called a soft open set. A soft set (F, E) is called soft closed in U if $(F, E)^c \in \tilde{\tau}$.

Definition [2.9] ^[1]

Let μ be the collection of supra soft sets over a universe U with a fixed set of parameters E, then μ is said to be a supra soft topology on U if

- 1) $\emptyset, U \in \mu$
 - 2) The union of any number of soft sets in μ belongs to μ .
- The triplet (U, μ , E) is called a supra soft topological space.

Every member of μ is called a supra soft open set. A soft set (F, E) is called supra soft closed in U if $(F, E)^c \in \mu$.

Definition [2.10] ^[15]

Let (U, μ , E) be a supra soft topological space and (F,E) be a supra soft set over X.

- (1) The supra soft closure of (F,E) is the supra soft $cl(F,E) = \bigcap \{(G,E): (G,E) \text{ is supra soft closed and } (F,E) \subseteq (G,E)\}$.
 - (2) The supra soft interior of (F,E) is the supra soft $int(F,E) = \bigcup \{(H,E): (H,E) \text{ is supra soft closed and } (H,E) \subseteq (F,E)\}$
- Clearly, $cl(F,E)$ is the smallest supra soft closed set over X which contains (F,E) and $int(F,E)$ is the largest supra soft open set over X which contained in (F,E).

Definition [2.11] ^[15]

Let (U, μ , E) be a supra soft topological space over U. A soft set (F, E) is called a supra soft generalized pre-regular closed set (supra soft gpr-closed) in U if $pcl(F,E) \subseteq (G, E)$ whenever $(F,E) \subseteq (G,E)$ and (G,E) is supra soft regular open in U.

3. Supra Soft π_g - closed sets in soft supra topological spaces.

Definition: 3.1 Finite union of supra soft regular open set in (X, μ ,E) is supra soft- π -open in (X, μ , E).

Definition: 3.2 Let (X, μ , E) be a supra soft topological space. A soft set (F, E) is called a supra soft π_g - closed set in X, if $cl^\mu(F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft π -open sets in X.

Definition: 3.3 Let (U, μ , E) be a supra soft topological space and (F,E) be a supra soft set over X.

- 1) The supra soft pre closure of (F, E) is the supra soft $pcl(F,E) = \bigcap \{(G,E): (G,E) \text{ is supra soft closed and } (F,E) \subseteq (G,E)\}$.
- 2) The supra soft pre interior of (F, E) is the supra soft pre $int(F,E) = \bigcup \{(H,E): (H,E) \text{ is supra soft closed and } (H,E) \subseteq (F,E)\}$

Clearly, $cl(F,E)$ is the smallest supra soft closed set over X which contains (F,E) and $int(F,E)$ is the largest supra soft open set over X which contained in (F,E).

Definition: 3.4 Let (X, μ , E) be a supra soft topological space. A soft supra set (F, E) is called,

- 1) A supra soft π_{gp} - closed set if $pcl^\mu(F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft π -open sets in X.

- 2) A supra soft π gr- closed set if $\text{rcl}^\mu (F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft π -open sets in X .
- 3) A supra soft gsr- closed set if $\text{scl}^\mu (F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft regular-open sets in X .
- 4) A supra soft π gs- closed set if $\text{scl}^\mu (F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft π -open sets in X .
- 5) A supra soft π gb- closed set if $\text{bcl}^\mu (F,E) \subseteq (G,E)$ whenever $(F, E) \subseteq (G, E)$ and (G, E) is a supra soft π -open sets in X .

Theorem 3.5: Every supra soft closed set is supra soft π g-closed.

Proof: Let $(F, E) \subseteq (G, E)$ and (G, E) be supra soft π - open. Since (F, E) is supra soft - closed set, we have $\text{cl}^\mu (F,E) = (F,E)$. Thus $\text{cl}^\mu (F,E) \subseteq (G,E)$. Hence (F,E) is supra soft π g- closed.

Remark 3.6: The converse of the above need not be true as seen by the following example.

Example 3.7

Let $X = \{h_1, h_2, h_3, h_4\}$, $E = \{e_1, e_2\}$
 $F_1(e_1) = \{h_3\}$, $F_1(e_2) = \{h_1\}$
 $F_2(e_1) = \{h_4\}$, $F_2(e_2) = \{h_2\}$
 $F_3(e_1) = \{h_3, h_4\}$, $F_3(e_2) = \{h_1, h_2\}$
 $F_4(e_1) = \{h_1, h_4\}$, $F_4(e_2) = \{h_2, h_4\}$
 $F_5(e_1) = \{h_2, h_3, h_4\}$, $F_5(e_2) = \{h_1, h_2, h_3\}$
 $F_6(e_1) = \{h_1, h_3, h_4\}$, $F_6(e_2) = \{h_1, h_2, h_4\}$
 $\mu = \{\tilde{\phi}, \tilde{X}, (F_1, E), (F_2, E), \dots, (F_6, E)\}$ defines a supra soft topology on X .
 Where $(A, E) = \{\{\phi\}, \{h_4\}\}$ is supra soft π g- closed set, but not supra soft closed.

Theorem 3.8: Every supra soft π g - closed set is supra soft π gp- closed

Proof: Let $(F,E) \subseteq (G,E)$, where (G,E) is supra soft π - open. Since (F, E) is supra soft π g-closed, we have $\text{cl}^\mu (F,E) \subseteq (G,E)$. Hence $\text{pcl}^\mu(F,E) \subseteq \text{cl}^\mu(F,E) \subseteq (G,E)$. Therefore, $\text{pcl}^\mu(F,E) \subseteq (G,E)$. Then (F,E) is supra soft π gp- closed.

Remark 3.9: The converse of the above theorem need not be true as seen by the following example.

Example 3.10

In example 3.7 $(A,E) = \{\{h_4\}, \{h_4\}\}$ is supra soft π gp-closed, but not supra soft π g closed.

Theorem 3.11: Every supra soft π g - closed set is supra soft π gs closed.

Proof: Let (F,E) be supra soft π g- closed and $(F,E) \subseteq (G,E)$, where (G,E) is supra soft π - open. Since (F,E) is supra soft π g closed, we have $\text{cl}^\mu(F,E) \subseteq (G,E)$. Also, $\text{scl}^\mu (F,E) \subseteq \text{cl}^\mu (F,E) \subseteq (G,E)$. Therefore $\text{scl}^\mu (F, E) \subseteq (G, E)$. Then (F,E) is supra soft π gs- closed.

Remark 3.12: The converse of the above need not be true as seen in the following example.

Example 3.13

In example 3.7, $(A,E) = \{\{h_3\}, \{h_1\}\}$ is supra soft π gs-closed, but not supra soft π g- closed.

Theorem 3.14: Every supra soft π gr- closed set is supra soft π g closed.

Proof: Let $(F, E) \subseteq (G,E)$ and (G,E) be supra soft π - open. Since (F, E) is supra soft π gr- closed. We have $\text{rcl}^\mu (F,E) \subseteq (G,E)$. Hence $\text{cl}^\mu (F, E) \subseteq \text{rcl}^\mu (F,E) \subseteq (G,E) \Rightarrow \text{cl}^\mu(F,E) \subseteq (G,E)$. Then (A, E) is supra soft π g - closed.

Remark 3.15: The converse of the above need not be true as seen in the following example.

Example 3.16:

In example 3.7 $(A, E) = \{\{\phi\}, \{h_4\}\}$ is supra soft π g -closed but not supra soft π gr- closed.

Theorem 3.17: Every supra soft π g - closed set is supra soft gsr closed.

Proof: Let (F,E) be supra soft π g- closed and $(F,E) \subseteq (G,E)$, where (G,E) is supra soft regular open. By assumption we have $\text{cl}^\mu (F, E) \subseteq (G,E)$. Hence $\text{scl}^\mu (F,E) \subseteq \text{cl}^\mu (F,E) \subseteq (G,E)$. Therefore $\text{scl}^\mu (F, E) \subseteq (G, E)$. Then (F,E) is supra soft gsr - closed.

Remark 3.18: The converse of the above need not be true as seen in the following example.

Example 3.19:

In example 3.7, $(A,E) = \{\{\phi\}, \{h_2, h_4\}\}$ is supra soft gsr-closed, but not supra soft π g- closed.

Theorem 3.20:

Every supra soft π g - closed set is supra soft π gbclosed.

Proof: Let $(F,E) \subseteq (G,E)$ and (G,E) is supra soft π - open. Since (F,E) be supra soft π g- closed and since every supra soft closed set is supra soft b^μ -closed, we have $\text{bcl}^\mu (F,E) \subseteq \text{cl}^\mu(F,E) \subseteq (G,E)$. Therefore $\text{bcl}^\mu (F, E) \subseteq (G, E)$. Then (F,E) is supra soft π gb - closed.

Remark 3.21: The converse of the above need not be true.

Example 3.22

In example 3.7, $(A,E) = \{\{h_1, h_4\}, \{h_2, h_4\}\}$ is supra soft π gb-closed but not supra soft π g- closed.

Theorem 3.23: Every supra soft π g - closed set is supra soft gpr closed.

Proof: Let $(F, E) \subseteq (G,E)$, where (G,E) is supra soft regular-open. Since (F, E) is supra soft π g- closed, we have $\text{cl}^\mu (F, E) \subseteq (G, E)$. Hence $\text{pcl}^\mu (F,E) \subseteq \text{cl}^\mu(F,E) \subseteq (G,E)$. Therefore, $\text{pcl}^\mu (F,E) \subseteq (G,E)$. Then (F, E) is supra soft gpr - closed.

Remark 3.24: The converse of the above need not be true as seen in the following example.

Example 3.25: In example 3.7, $(A,E) = \{\{h_3\}, \{h_4\}\}$ is supra soft gpr -closed but not supra soft π g- closed.

Theorem 3.26: Let (X, μ, E) be a supra soft topological space and (F, E) be a supra soft set over X . If a supra soft set (F, E) is a supra soft πg – closed set, then $cl^\mu(F, E) - (F, E)$ contains only null supra soft π - closed set.

Proof: Suppose that (F, E) is a supra soft πg - closed set. Let (H, E) be a supra soft π closed subset of $cl^\mu(F, E) - (F, E)$. Then $(H, E) \subseteq cl^\mu(F, E) \cap (F, E)^c$. So $cl^\mu(F, E) \subseteq (H, E)^c$. But (F, E) is a supra soft πg – closed set, $\Rightarrow cl^\mu(F, E) \subseteq (H, E)^c$. Consequently,
 $(H, E) \subseteq [cl^\mu(F, E)]^c$ (1)
 We have already, $(H, E) \subseteq cl^\mu(F, E)$ (2)
 From (1) and (2), $(H, E) \subseteq cl^\mu(F, E) \cap [cl^\mu(F, E)]^c = \Phi$. Thus $(H, E) = \Phi$. Therefore $cl^\mu(F, E) - (F, E)$ contains only null supra soft π – closed set.

Theorem 3.27
 Let (X, μ, E) be a supra soft topological space and (F, E) be a supra soft πg – closed set in X . (F, E) is supra soft π – closed. iff, $cl^\mu(int^\mu(F, E)) - (F, E)$ is supra soft π – closed.

Proof: Let (F, E) be supra soft πg – closed set. If (F, E) is supra soft π – closed then $cl^\mu(int^\mu(F, E)) - (F, E) = \Phi$. Since Φ is always supra soft π – closed. Then $cl^\mu(int^\mu(F, E)) - (F, E)$ is supra soft π – closed. Conversely, suppose that $cl^\mu(int^\mu(F, E)) - (F, E)$ is supra soft π – closed. Since (F, E) is supra soft πg closed and $cl^\mu(F, E) - (F, E)$ contains supra soft π – closed set. $cl^\mu(int^\mu(F, E)) - (F, E)$ then $cl^\mu(int^\mu(F, E)) - (F, E) = \Phi$. Hence $cl^\mu(int^\mu(F, E)) = (F, E)$. Therefore (F, E) is supra soft π – closed.

Theorem 3.28
 Let (X, μ, E) be a supra soft topological space, (F, E) and (G, E) supra soft sets over X . If (F, E) is supra soft πg – closed set and $(F, E) \subseteq (G, E) \subseteq cl^\mu(F, E)$, then $cl^\mu(G, E) - (G, E)$ contains only null supra soft π - closed set.

Proof: If $(F, E) \subseteq (G, E)$, then $(G, E)^c \subseteq (F, E)^c$ (1)
 If $(G, E) \subseteq cl^\mu(F, E)$ then $cl^\mu(G, E) = cl^\mu(cl^\mu(F, E)) = cl^\mu(F, E)$ (2)
 that is, $cl^\mu(G, E) \subseteq cl^\mu(F, E)$ from (1) and (2).
 $[cl^\mu(G, E) \cap (G, E)^c] \subseteq [cl^\mu(F, E) \cap (F, E)^c] \Leftrightarrow [cl^\mu(G, E) - (G, E)] \subseteq [cl^\mu(F, E) - (F, E)]$
 Now (F, E) is supra soft πg – closed set. Hence $cl^\mu(F, E) - (F, E)$ contains only null supra soft π – closed set, neither does $cl^\mu(G, E) - (G, E)$.

Definition 3.29
 Let (X, μ, E) be a supra soft topological spaces. A supra soft set (F, E) is called supra soft πg – open set in X , if $(F, E)^c$ is supra soft πg – closed set.

Theorem 3.30
 A supra soft set (F, E) is supra soft πg – open set in a supra soft topological space (X, μ, E) , if and only if $(H, E) \subseteq int^\mu(F, E)$ whenever (H, E) is supra soft π closed set in X and $(H, E) \subseteq (F, E)$.

Proof: Let $(H, E) \subseteq int^\mu(F, E)$ whenever (H, E) is supra soft π – closed set in X . $(H, E) \subseteq (F, E)$ and $(K, E) = (F, E)^c$. Suppose that $(K, E) \subseteq (G, E)$ where (G, E) is supra soft π – open set.
 Now $(F, E)^c \subseteq (G, E) \Rightarrow (H, E) = (G, E)^c \subseteq (F, E)$ and (H, E) is supra soft π – closed set.

$\Rightarrow (H, E) \subseteq int^\mu(F, E)$.
 Also $(H, E) \subseteq int^\mu(F, E) \Rightarrow [int^\mu(F, E)]^c \subseteq (H, E)^c = (G, E) \Rightarrow [int^\mu[(K, E)^c]]^c \subseteq (G, E)$ or equivalently $cl^\mu(F, E) \subseteq (G, E)$. Thus (K, E) is supra soft πg – closed set. Hence we obtain (F, E) is supra soft πg - open set.
 Conversely, suppose that (F, E) is supra soft πg – open set, $(H, E) \subseteq (F, E)$ and (H, E) is supra soft π – closed set. Then, $(H, E)^c$ is supra soft π open set. Then, $(F, E)^c \subseteq (H, E)^c$. Since $(F, E)^c$ is supra soft πg – closed set, $cl^\mu((F, E)^c) \subseteq (H, E)^c$. Therefore, $(H, E) \subseteq (cl^\mu[(F, E)^c])^c = int^\mu(F, E)$.

Theorem 3.31
 Let $(A, E) \subseteq (B, E) \subseteq cl^\mu(A, E)$ and (A, E) is a supra soft πg – closed set of (X, E) then (B, E) is also supra soft πg – closed set of (X, E) .

Proof: Since (A, E) is supra soft πg – closed set of (X, E) . So $cl^\mu(A, E) \subseteq U$, whenever $(A, E) \subseteq U$, U being an supra soft π – open set of X . Let $(A, E) \subseteq (B, E) \subseteq cl^\mu(A, E)$. ie., $cl^\mu(A, E) = cl(B, E)$. Let if possible there exists an open subset V of (X, E) such that $(B, E) \subseteq V$. So, $cl^\mu(A, E) \subseteq V$. ie., $cl^\mu(B, E) \subseteq V$. Hence (B, E) is also a supra soft πg - closed set of (X, E) .

Theorem 3.32
 If $int^\mu(A, E) \subseteq (B, E) \subseteq (A, E)$ and (A, E) is a supra soft πg – open set of (X, μ, E) then (B, E) is also a supra soft πg open set of (X, E) .

Proof: $int^\mu(A, E) \subseteq (B, E) \subseteq (A, E)$ implies $(A, E)^c \subseteq (B, E)^c \subseteq cl(A, E)^c$. Given $(A, E)^c$ is supra soft πg – closed. $(B, E)^c$ is supra soft πg – closed. Therefore (B, E) is supra soft πg – open.

4. supra soft πg – separateness

Definition: 4.1: Let (U, μ, E) be a supra soft topological space over U and (F, E) be a supra soft set over U .

- (1) The supra soft πg closure of (F, E) is the supra soft $\pi g cl(F, E) = \bigcap \{(G, E): (G, E) \text{ is supra soft } \pi g \text{ closed and } (F, E) \subseteq (G, E)\}$.
- (2) The supra soft πg interior of (F, E) is the supra soft $\pi g int(F, E) = \bigcup \{(H, E): (H, E) \text{ is supra soft } \pi g \text{ open and } (H, E) \subseteq (F, E)\}$

Clearly, $\pi g cl(F, E)$ is the smallest supra soft πg closed set over U which contains (F, E) and $\pi g int(F, E)$ is the largest supra soft πg open set over U which contained in (F, E) .

Definition 4.2: Two non-null soft sets (G, E) and (H, E) of a supra soft topological space (X, μ, E) are said to be supra soft πg -separated sets if $(G, E) \cap \pi g cl^\mu(H, E) = \Phi$ and $\pi g cl^\mu(G, E) \cap (H, E) = \Phi$.

Definition 4.3 : A soft set (F, E) of a supra soft topological space (X, μ, E) is said to be supra soft πg -clopen set if it is both supra soft πg -open set and supra soft πg -closed set.

Remark 4.4

- 1) Each two supra soft πg -separated sets are always disjoint.
- 2) Each two disjoint soft sets, in which both of them either supra soft - πg open sets or supra soft- πg closed sets, are supra soft - πg separated.

Theorem 4.5: Let (G,E) and (H,E) be non-null soft sets of a supra soft topological space (X,μ,E) . Then the following statements hold:

- 1) If (G,E) and (H,E) are supra soft πg separated, $(G_1,E) \subseteq (G,E)$ and $(H_1,E) \subseteq (H,E)$, then (G_1,E) and (H_1,E) are supra soft πg separated sets.
- 2) If (G,E) and (H,E) are supra soft πg open sets, $(U,E) = (G,E) \cap (X,E) - (H,E)$ and $(V,E) = (H,E) \cap (X,E) - (G,E)$, then (U,E) and (V,E) are supra soft πg separated sets.

Proof:

- 1) Since $(G_1,E) \subseteq (G,E)$. Then, $\pi gcl^\mu(G_1,E) \subseteq \pi gcl^\mu(G,E)$. Hence $(H_1,E) \cap \pi gcl^\mu(G_1,E) \subseteq (H,E) \cap \pi gcl^\mu(G,E) = \varnothing$. Similarly, $(G,E) \cap \pi gcl^\mu(H_1,E) = \varnothing$. Thus (G_1,E) and (H_1,E) are supra soft πg -separated sets.
- 2) Let (G,E) and (H,E) be supra soft πg -open sets. Then $(X,E) - (G,E)$ and $(X,E) - (H,E)$ are supra soft πg -closed sets. Assume that, $(U,E) = (G,E) \cap (X,E) - (H,E)$ and $(V,E) = (H,E) \cap (X,E) - (G,E)$. Then

$(U,E) \subseteq (X,E) - (H,E)$ and $(V,E) \subseteq (X,E) - (H,E)$. Hence, $\pi gcl^\mu(U,E) \subseteq (X,E) - (H,E) \subseteq (X,E) - (V,E)$ and $\pi gcl^\mu(V,E) \subseteq (X,E) - (G,E) \subseteq (X,E) - (U,E)$. Consequently, $\pi gcl^\mu(U,E) \cap (V,E) = \varnothing$ and $\pi gcl^\mu(V,E) \cap (U,E) = \varnothing$. Therefore, (U,E) and (V,E) are supra soft πg -separated sets.

Theorem 4.6. Any two supra soft sets (G,E) and (H,E) of a supra soft topological space (X,μ,E) are supra soft πg -separated sets if and only if there exist supra soft πg -open sets (U,E) and (V,E) such that $(G,E) \subseteq (U,E)$, $(H,E) \subseteq (V,E)$ and $(G,E) \cap (V,E) = \varnothing$, $(H,E) \cap (U,E) = \varnothing$

Proof:

Necessity: Let (G,E) and (H,E) be supra soft πg -separated sets. Then, $(G,E) \cap \pi gcl^\mu(H,E) = \varnothing$. And $\pi gcl^\mu(G,E) \cap (H,E) = \varnothing$. Let $(V,E) = (X,E) - \pi gcl^\mu(G,E)$ and $(U,E) = (X,E) - \pi gcl^\mu(H,E)$. Thus, (U,E) and (V,E) are supra soft πg -open sets such that $(G,E) \subseteq (U,E)$, $(H,E) \subseteq (V,E)$, $(G,E) \cap (V,E) = \varnothing$ and $(H,E) \cap (U,E) = \varnothing$.

Sufficient: Let (U,E) , (V,E) be supra soft πg -open sets such that $(G,E) \subseteq (U,E)$, $(H,E) \subseteq (V,E)$ and $(G,E) \cap (V,E) = \varnothing$, $(H,E) \cap (U,E) = \varnothing$. Since $(X,E) - (H,E)$ and $(X,E) - (U,E)$ are supra soft πg -closed sets. Then, $\pi gcl^\mu(G,E) \subseteq (X,E) - (V,E) \subseteq (X,E) - (H,E)$ and $\pi gcl^\mu(H,E) \subseteq (X,E) - (U,E) \subseteq (X,E) - (G,E)$. Thus, $\pi gcl^\mu(G,E) \cap (H,E) = \varnothing$ and $\pi gcl^\mu(H,E) \cap (G,E) = \varnothing$.

This means that, (G,E) and (H,E) are supra soft πg -separated sets.

5. Supra soft πg - connected

Definition 5.1: Let (X,μ,E) be a supra soft topological space. A supra soft πg -separation of X is a pair of non-null proper supra soft πg -open sets in μ such that $(F,E) \cap (G,E) = \varnothing$ and $X = (F,E) \cup (G,E)$.

Definition 5.2: A supra soft topological space (X,μ,E) is said to be supra soft πg -connected if and only if there is no supra soft πg -separations of X . If (X,μ,E) has such supra soft πg -separations, then (X,μ,E) is said to be supra soft πg -disconnected.

Remark 5.3

- 1) \varnothing is always supra soft πg -connected.
- 2) If (G,E) , (H,E) are non-null supra soft πg -separated sets. Then, the pair (G,E) , (H,E) is called the supra soft πg -disconnection of X .

Theorem 5.4: Let (X,μ,E) be a supra soft topological space, then the following statements are equivalent:

- 1) X is supra soft πg -connected.
- 2) X can not be expressed as a supra soft union of two non-null disjoint supra soft πg -open sets.
- 3) X can not be expressed as a supra soft union of two non-null disjoint supra soft πg -closed sets.
- 4) There is no proper supra soft πg -clopen set in (X,μ,E) .
- 5) X can not be expressed as a supra soft union of two non-null supra soft πg -separated sets.

Proof:

- (1) \Leftrightarrow (2): It is obvious from Definition 5.2.
- (2) \Rightarrow (3): Suppose that $X = (F,E) \cup (G,E)$, for some supra soft πg -closed sets (F,E) and (G,E) such that $(F,E) \cap (G,E) = \varnothing$. Then, $(F,E) = (G,E)^c$. Which is supra soft πg -open set, $X = (G,E) \cup (G,E)^c$ and $(G,E) \cap (G,E)^c = \varnothing$, which is a contradiction with (2).
- (3) \Rightarrow (4): Suppose that there is a proper supra soft πg -clopen subset (F,E) of X . Then, $(F,E)^c$ is supra soft πg -clopen set, where $X = (F,E) \cup (F,E)^c$ and $(F,E) \cap (F,E)^c = \varnothing$. which is a contradiction with (3).
- (4) \Rightarrow (3): Suppose that $X = (F,E) \cup (G,E)$ for some supra soft πg -closed sets (F,E) and (G,E) such that $(F,E) \cap (G,E) = \varnothing$. Then, $(F,E) = (G,E)^c$ and $(G,E) = (F,E)^c$. Thus, (F,E) and (G,E) are proper supra soft πg -clopen sets, which is a contradiction with (4).
- (3) \Rightarrow (5): Suppose that $X = (H,E) \cup (G,E)$ for some supra soft πg -separated sets (H,E) and (G,E) . Then, $(G,E) \cap \pi gcl^\mu(H,E) = \varnothing$ and $\pi gcl^\mu(G,E) \cap (H,E) = \varnothing$. It follows that, $(H,E) \cap (G,E) = \varnothing$. Hence, $(H,E) = (G,E)^c$ and $(G,E) = (H,E)^c$. Therefore, $\pi gcl^\mu(H,E) \subseteq (G,E) = (H,E)$ and $\pi gcl^\mu(G,E) \subseteq (H,E) = (G,E)$. But, $(H,E) \subseteq \pi gcl^\mu(H,E)$ and $(G,E) \subseteq \pi gcl^\mu(G,E)$. Thus, (H,E) and (G,E) are supra πg -closed soft sets, which is a contradiction with (3).
- (5) \Rightarrow (1): Suppose that $X = (F,E) \cup (G,E)$ for some supra soft πg -open sets (F,E) and (G,E) such that $(F,E) \cap (G,E) = \varnothing$. Then $(F,E) = (G,E)^c$ and $(G,E) = (F,E)$. Thus, (F,E) and (G,E) are supra soft πg -clopen sets. Hence, (F,E) and (G,E) are supra soft πg -separated sets, which is a contradiction with (5).

Corollary 5.5: Let (X,μ,E) be a supra soft topological space, then the following statements are equivalent:

- 1) X is supra soft πg -connected.
- 2) If $X = (F,E) \cup (G,E)$, for some supra soft πg -open sets (F,E) and (G,E) such that $(F,E) \cap (G,E) = \varnothing$. Then, either $(F,E) = \varnothing$ or $(G,E) = \varnothing$.
- 3) If $X = (F,E) \cup (G,E)$ for some supra soft πg -closed sets (F,E) and (G,E) such that $(F,E) \cap (G,E) = \varnothing$. Then, either $(F,E) = \varnothing$ or $(G,E) = \varnothing$.

Proof:

Obvious from Theorem 5.4.

6. References

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